

Inferences of Asymptotic Notations

1. $A \neq \Theta(B) \Leftrightarrow A \neq \Omega(B) \vee A \neq O(B)$ (*DeMorgan's Law*)
2. $A = \omega(B) \rightarrow A = \Omega(B)$ (*By Definition*)
3. $A \neq \Omega(B) \rightarrow A \neq \omega(B)$ (*Contrapositive of Rule 2*)
4. $A = \omega(B) \rightarrow A \neq O(B)$ (*Complement*) $\rightarrow A \neq \Theta(B)$ (*By Rule 1*)
5. $A = o(B) \rightarrow A = O(B)$ (*By Definition*)
6. $A \neq O(B) \rightarrow A \neq o(B)$ (*Contrapositive of Rule 5*)
7. $A = o(B) \rightarrow A \neq \Omega(B)$ (*Complement*) $\rightarrow A \neq \Theta(B)$ (*By Rule 1*)